

OXFORD CAMBRIDGE AND RSA EXAMINATIONS
GCSE (9–1)
J560/06

MATHEMATICS
Paper 6 (Higher Tier)

MONDAY 12 NOVEMBER 2018: Morning
TIME ALLOWED: 1 hour 30 minutes
plus your additional time allowance

MODIFIED ENLARGED

First name		Last name	
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Centre number						Candidate number				
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YOU MAY USE:

- a scientific or graphical calculator**
- geometrical instruments**
- tracing paper**

READ INSTRUCTIONS OVERLEAF



INSTRUCTIONS

Use black ink. You may use an HB pencil for graphs and diagrams.

Complete the boxes on the front page with your name, centre number and candidate number.

Answer ALL the questions.

Read each question carefully before you start to write your answer.

Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.

Write your answer to each question in the space provided. If additional space is required, use the lined page(s) at the end of this booklet. The question number(s) must be clearly shown.

INFORMATION

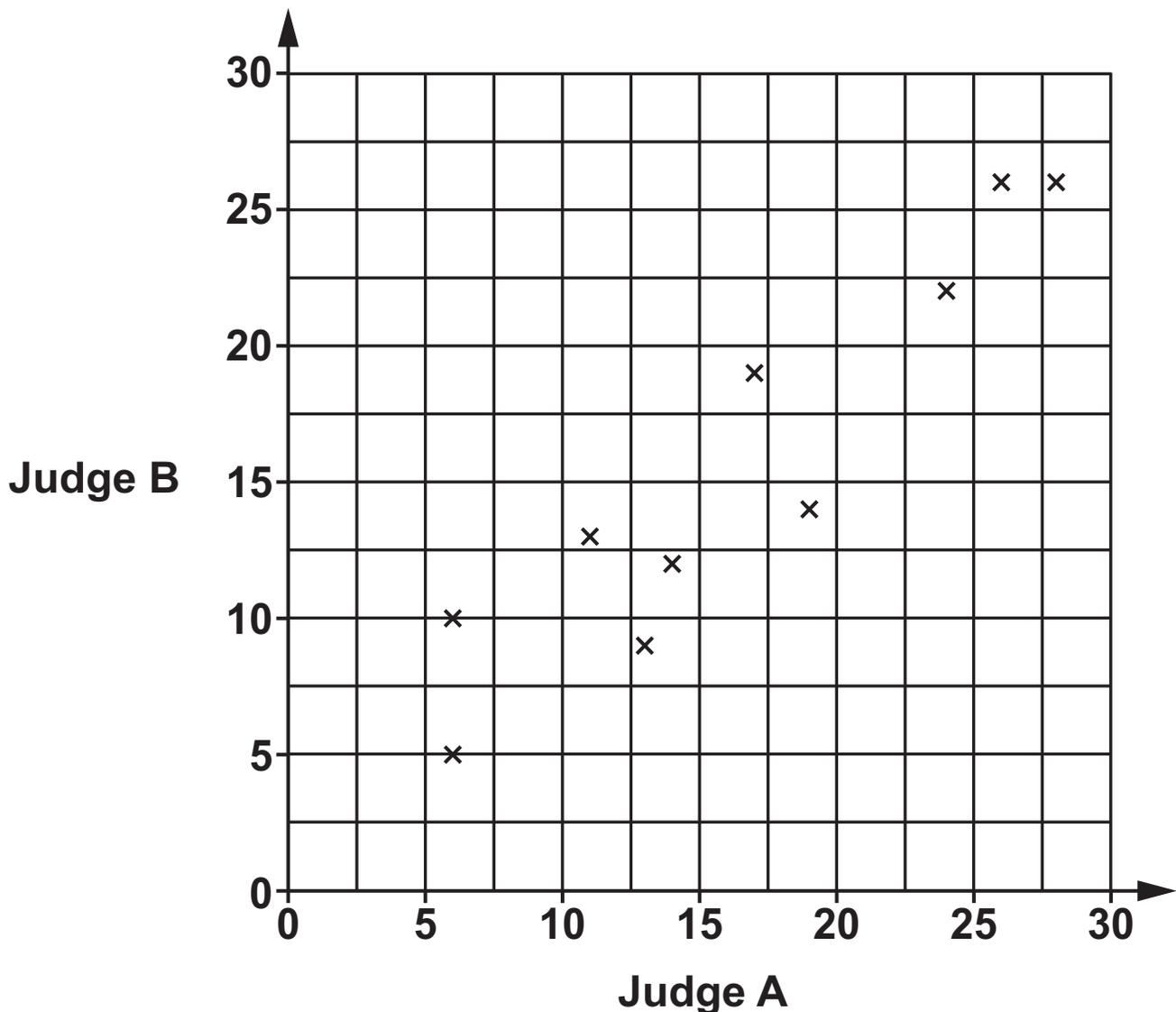
The total mark for this paper is 100.

The marks for each question are shown in brackets [].

Use the π button on your calculator or take π to be 3.142 unless the question says otherwise.

Answer ALL the questions.

- 1 In a dance competition, two judges each award scores out of 30.
The scatter diagram shows the scores awarded to the first 10 dancers.



- (a) Here are the scores for the next two dancers.

Judge A	21	7
Judge B	18	8

Plot their scores on the scatter diagram. [1]

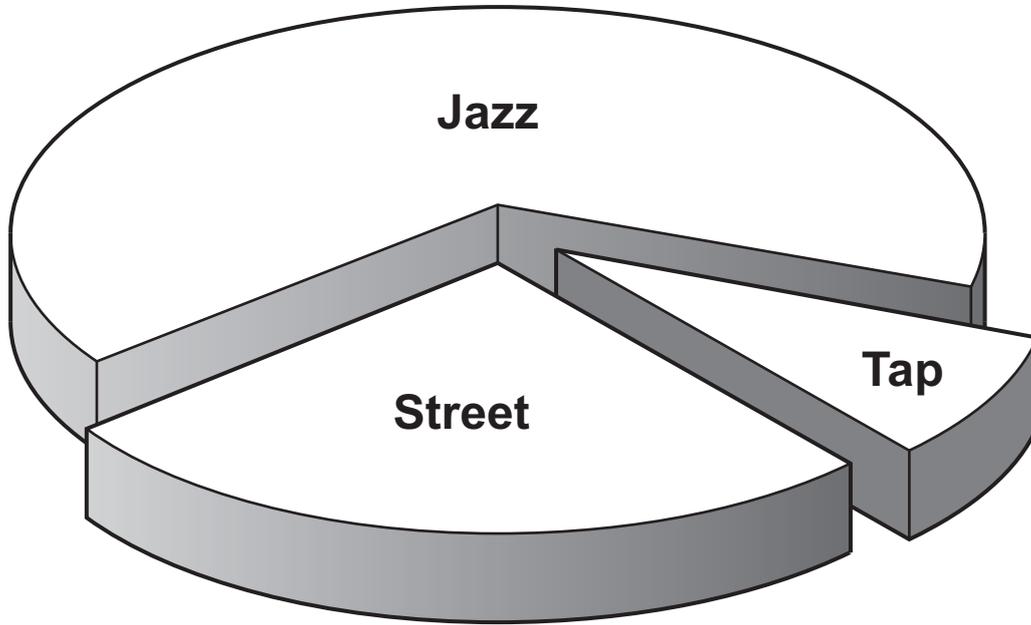
(b) Dancers who are awarded a score of more than 20 by BOTH judges receive a medal.

For the 12 dancers, express the ratio of medal winners to non-medal winners in its simplest form.

(b) _____ : _____ [3]

(c) This chart shows the types of dance performed by the 12 dancers.

3 performed a street dance, 8 performed a jazz dance and 1 performed a tap dance.



Why is this diagram misleading?

[1]

- 2 The police record the speed of vehicles passing a speed checkpoint.
The speeds are recorded in the table below.

Speed (s mph)	Number of vehicles		
$0 < s \leq 20$	5		
$20 < s \leq 40$	8		
$40 < s \leq 50$	37		
$50 < s \leq 60$	47		
$60 < s \leq 80$	3		

- (a) Calculate an estimate of the mean speed of the vehicles.

(a) _____ mph [4]

(b) Explain why it is not possible to use the information from this table to calculate the EXACT value of the mean speed.

[1]

3 A newborn baby has an approximate mass of 3.5 kilograms.

A human cell has an approximate mass of 2.7×10^{-11} grams.

Use these values to estimate the number of human cells in a newborn baby.

Give your answer in standard form, correct to 2 significant figures.

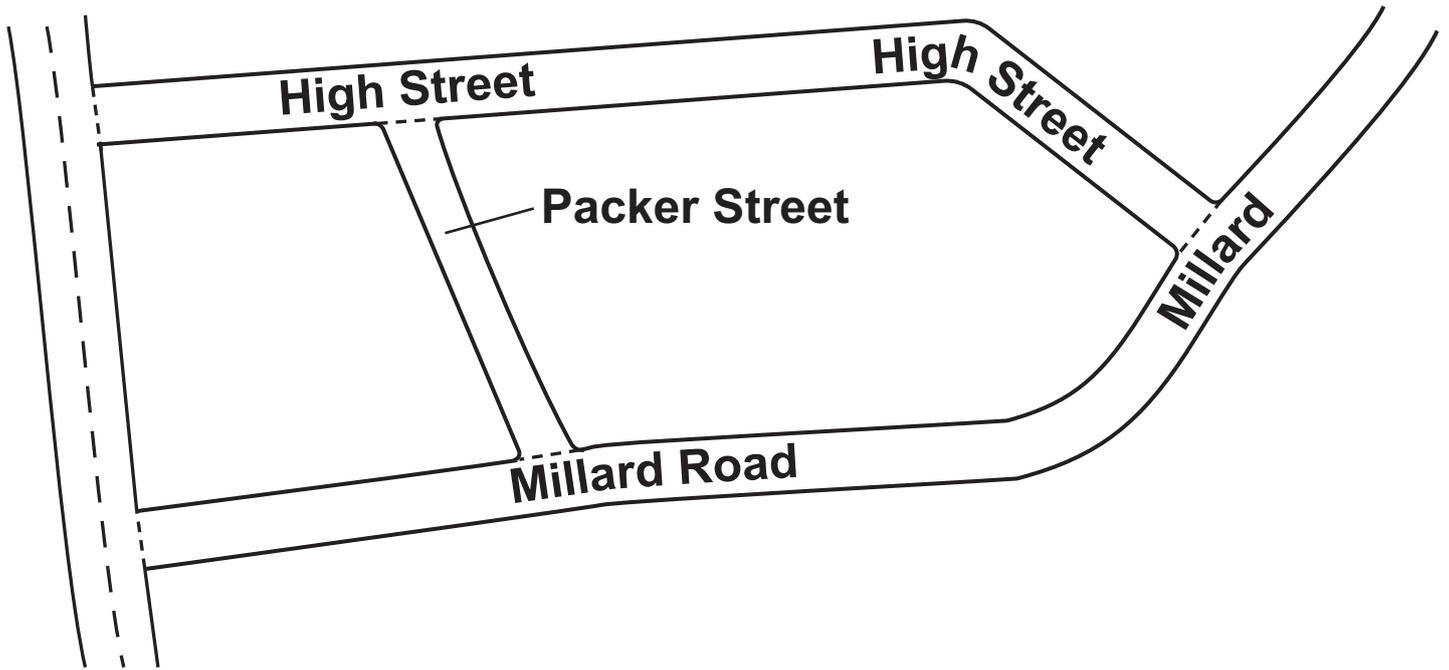
[5]

4 Use the symbols $<$, \leq , $=$, $>$, or \geq to complete this statement.

If $x = 4.7$, TRUNCATED to 1 decimal place, then

4.7 _____ x _____ 4.8 [2]

5 This map shows part of a village.



Neil knows that Packer Street is 180 m long in real life.

(a) Neil measures the map.

He says

Packer Street is 3.5cm long.

High Street is 11.2cm long.

Therefore, I calculate that High Street is 576m long in real life.

Use Neil's figures to show that the answer to his calculation is correct. [3]

(b) Jodie measures the same map.

She says

I think Packer Street is longer than Neil's measurement of 3.5cm.

Therefore, High Street must be longer than 576m in real life.

Is Jodie's reasoning correct?

Show how you decide.

[2]

(c) On another map, Packer Street is 2.4 cm long.

Express the scale of this map in the form 1 : n .

(c) 1 : _____ [2]

- 6 In a box of mixed nuts, the total number of almonds, cashews and peanuts is 1025.
The ratio of almonds to cashews is 1 : 3.
The ratio of cashews to peanuts is 5 : 7.**

Calculate the number of cashews in the box.

_____ **[4]**

7 The probability that any postcard posted in Portugal on Monday is delivered to the UK within a week is 0.62.

The probability that any postcard posted in Portugal on Friday is delivered to the UK within a week is 0.41.

**(a) Anna is on holiday in Portugal.
She posts 15 postcards to the UK on Monday.**

How many of her postcards can she expect to be delivered within a week?

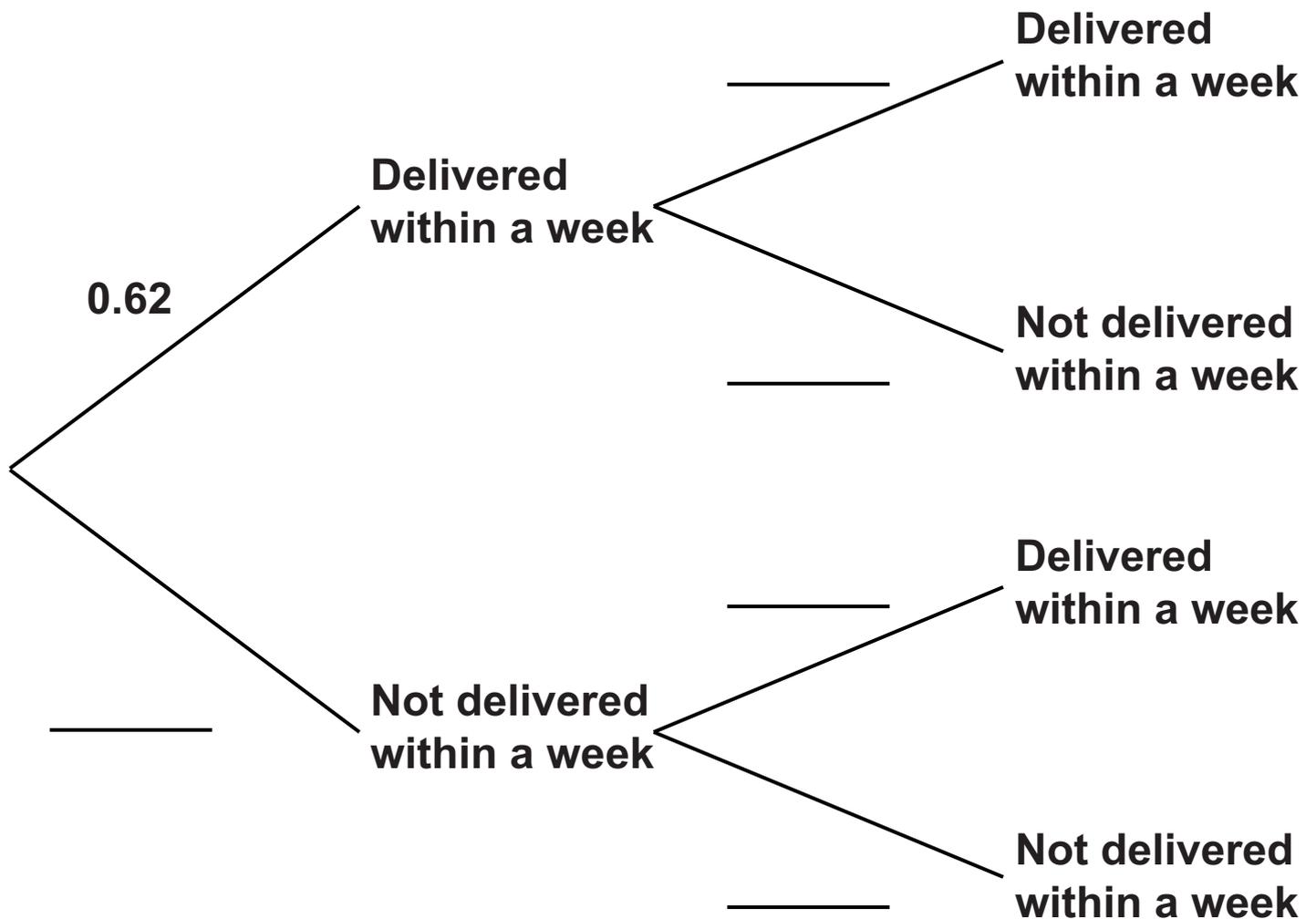
(a) _____ [2]

**(b) Sergio is in Portugal.
He posts one postcard to the UK on Monday.
He posts another postcard to the UK on Friday.**

- (i) Complete the probability tree to show the possible outcomes for the postcards. [2]

**MONDAY'S
POSTCARD**

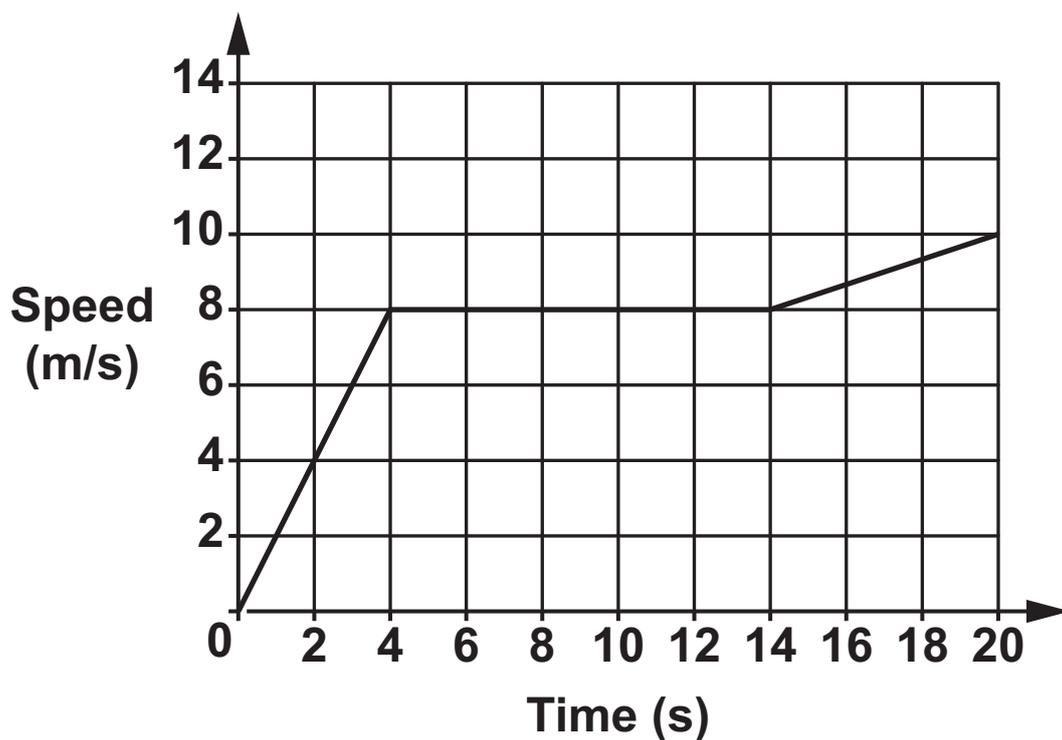
**FRIDAY'S
POSTCARD**



- (ii) Calculate the probability that only one of Sergio's postcards is delivered within a week.

(b)(ii) _____ [3]

- 8 The graph shows the speed of a cyclist during 20 seconds of a journey.



(a) Find the acceleration of the cyclist

(i) for the first 4 seconds

(a)(i) _____ m/s^2 [2]

(ii) between 4 seconds and 14 seconds.

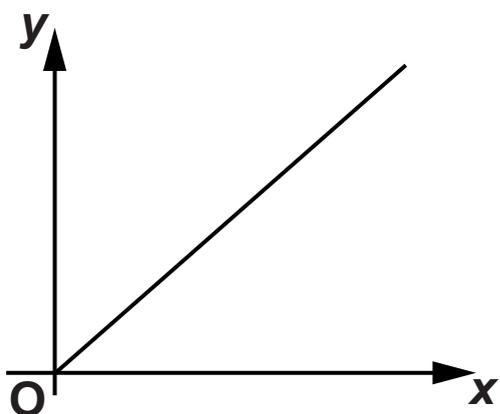
(ii) _____ m/s^2 [1]

(b) Work out the distance travelled by the cyclist during the 20 seconds.

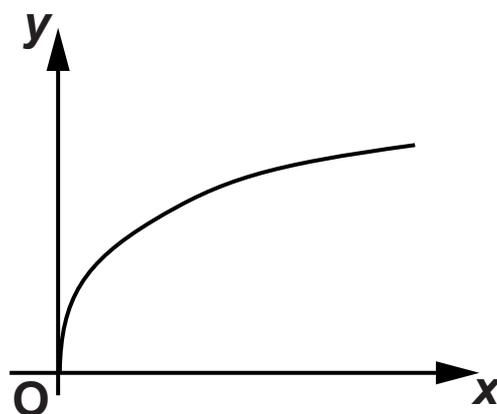
(b) _____ m [4]

9 These graphs show different relationships between the variables x and y .

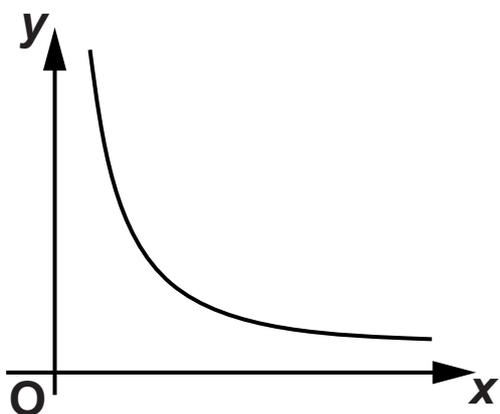
Graph A



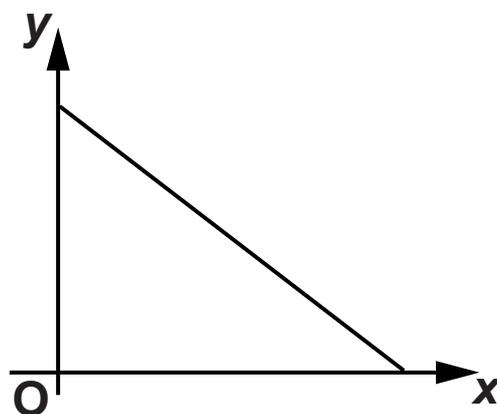
Graph B



Graph C



Graph D



Identify the graph which shows the following.

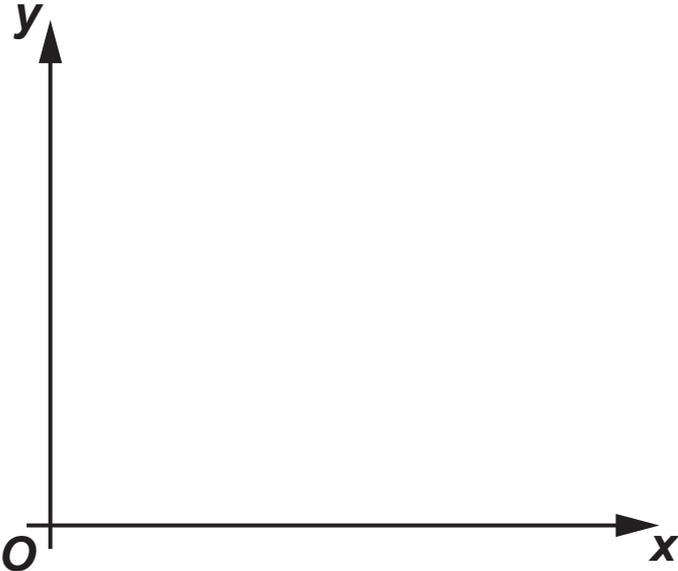
(a) y is directly proportional to x .

(a) Graph _____ [1]

(b) y is inversely proportional to x .

(b) Graph _____ [1]

10 Sketch a graph which shows that y is directly proportional to x^2 . [2]

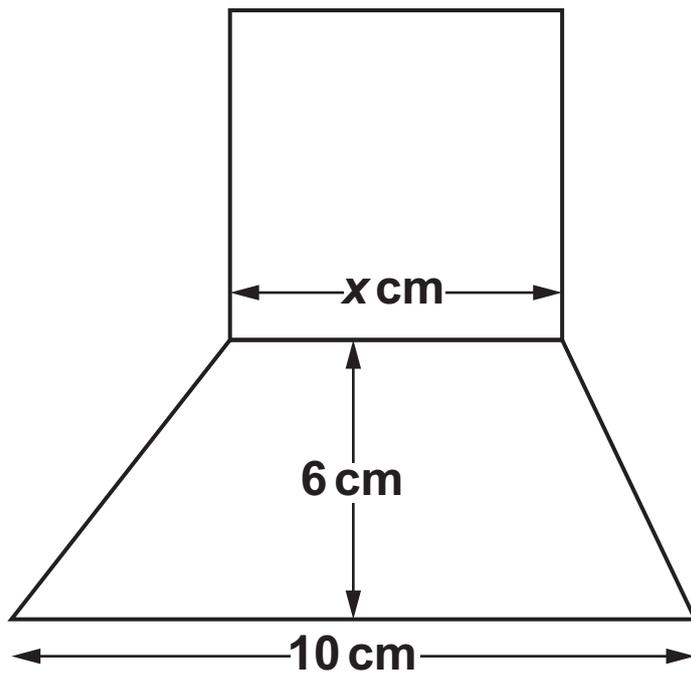


- 11 A regular polygon has n sides.
The polygon's interior angle is 5 times the size of its exterior angle.

Find n .

$$n = \underline{\hspace{2cm}} [5]$$

- 12 In the diagram, the square and the trapezium share a common side of length x cm.



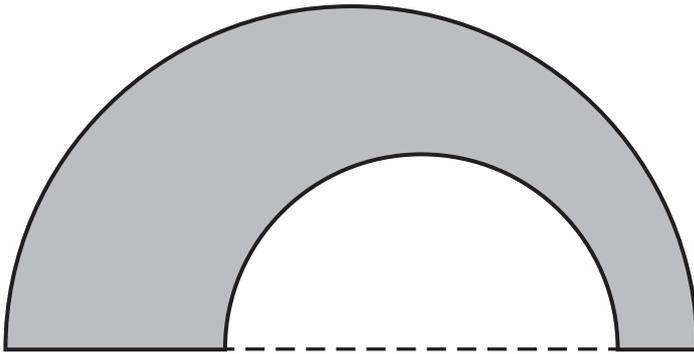
NOT TO SCALE

The area of the square is equal to the area of the trapezium.

Work out the value of x .

$x =$ _____ [6]

- 13 The shape below is formed from two semicircles and a straight line.



NOT TO SCALE

The radius of the large semicircle is 8 cm.
The radius of the small semicircle is t cm.

Find an expression, in terms of t , for the EXACT PERIMETER of the shaded shape.

_____ cm [3]

14 (a) WITHOUT USING A CALCULATOR, show that

$0.\dot{1}\dot{9}$ can be written as $\frac{19}{99}$. [3]

(b) Explain how $\frac{19}{99} = 0.\dot{1}\dot{9}$ can be used to find $\frac{19}{990}$ as a decimal and write down its value.

$$\frac{19}{990} = \underline{\hspace{2cm}} \quad [2]$$

- 15 Use the formula $x_{n+1} = \frac{(x_n)^3}{30} + 2$ with $x_1 = 2$ to calculate x_2 and x_3 .
Round your answers correct to 4 decimal places.

$x_2 =$ _____ and $x_3 =$ _____ [3]

- 16 A £1 coin weighs 8.75g, correct to the nearest 0.01 g. Mitul weighs the contents of a large bag of £1 coins. The coins weigh 2.63kg, correct to the nearest 10g.

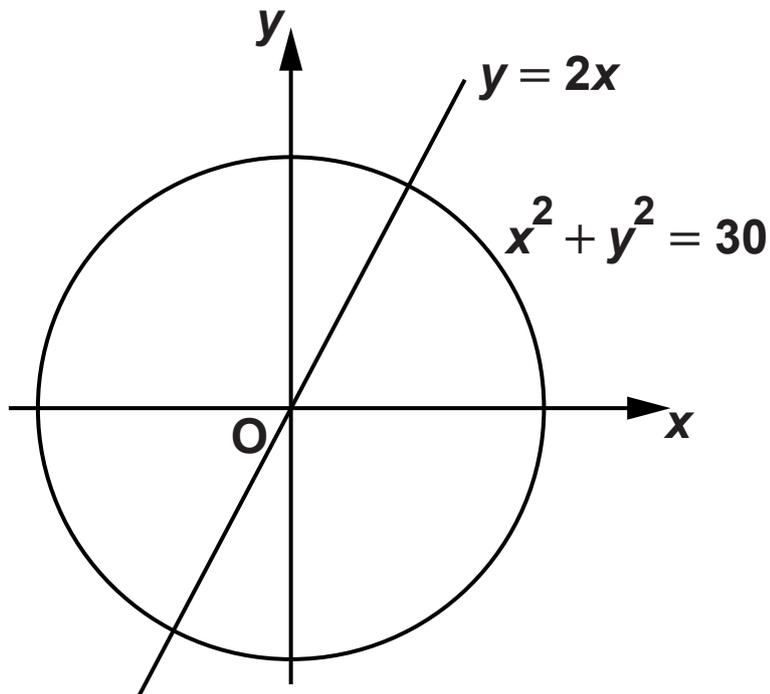
Mitul says

I am sure that the bag contains exactly £300 because, using bounds,
 $2625 \div 8.755 = 299.8$ to 1 decimal place.

Show that Mitul may not be correct.

[3]

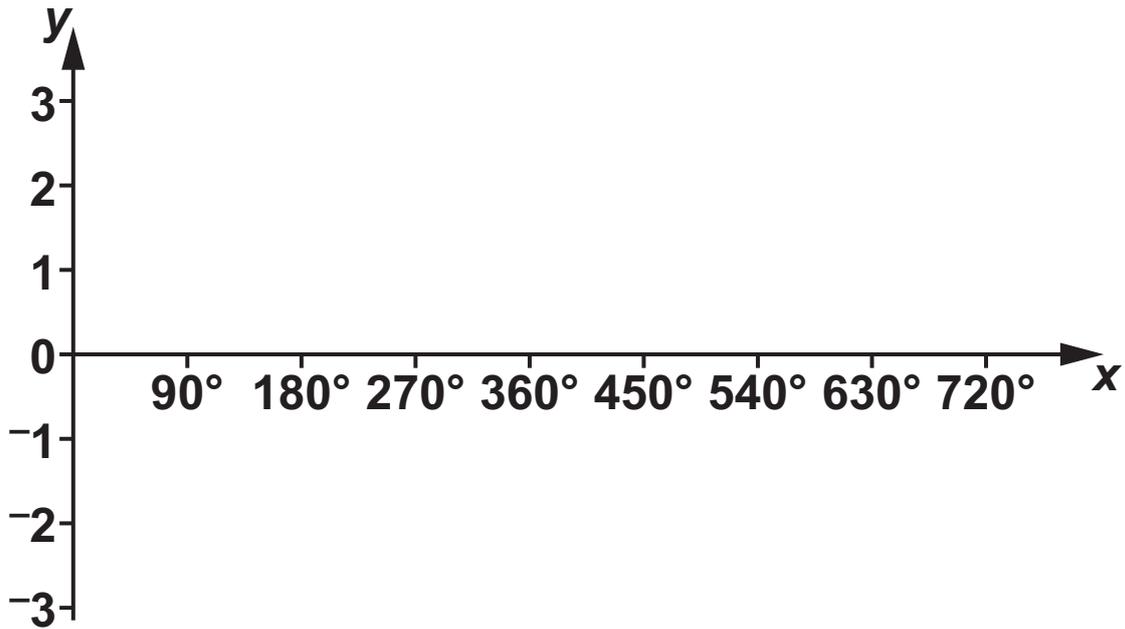
- 17 Find the exact coordinates of the two intersections of the line $y = 2x$ and the circle $x^2 + y^2 = 30$.



NOT TO SCALE

(_____ , _____) and (_____ , _____) [5]

- 18 (a) Sketch the graph of $y = \cos x + 1$ for $0^\circ \leq x \leq 720^\circ$. [3]



- (b) Explain why the equation $\cos x + 1 = 2.7$ has no solutions.

[1]

19 In this triangle:

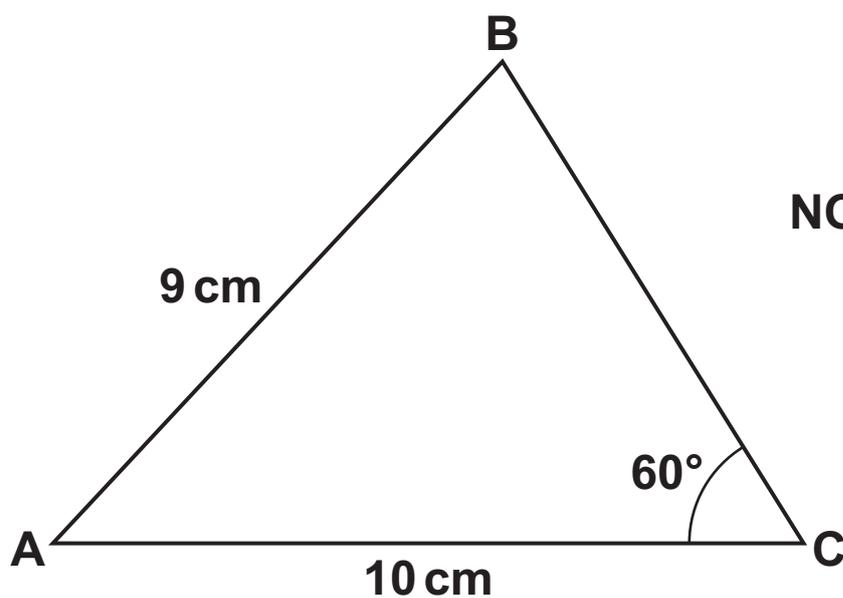
$$AB = 9 \text{ cm}$$

$$AC = 10 \text{ cm}$$

$$BC > 5 \text{ cm}$$

$$\text{angle } BCA = 60^\circ$$

$$\text{angle } ABC < 90^\circ.$$



NOT TO SCALE

Calculate the area of triangle ABC.

_____ **cm² [6]**

20 (a) \mathbf{b} is a vector.

Given that $\mathbf{b} + \begin{pmatrix} 5 \\ 2 \end{pmatrix}$ is parallel to $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$, find two possible answers for \mathbf{b} .

$$(a) \mathbf{b} = \begin{pmatrix} \quad \\ \quad \end{pmatrix} \text{ or } \begin{pmatrix} \quad \\ \quad \end{pmatrix} [3]$$

(b) Given that

$$m \begin{pmatrix} 4 \\ 1 \end{pmatrix} + n \begin{pmatrix} 5 \\ 2 \end{pmatrix} = \begin{pmatrix} 12 \\ 6 \end{pmatrix}$$

find the value of m and the value of n .

(b) $m =$ _____

$n =$ _____ **[5]**

21 Show that $\frac{5x}{x+5} + \frac{25}{x-7} - \frac{300}{(x+5)(x-7)}$ simplifies to an integer. [6]

END OF QUESTION PAPER

